APPLICATION OF EVOLUTIONARY ALGORITHM FOR OPTIMIZATION OF THE LAYOUT OF A MULTI-BRANCHED NETWORK CONSTRUCTED WITH TRUSS-Z SYSTEM

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Abstract. This paper concerns with the optimization of a planar layout of the multi-branched network created with Truss-Z (TZ) linking six terminals in an environment with two rectangular obstacles. This multi-objective optimization problem has two criteria: the number of modules to be the smallest (economical optimization) and none of the modules should collide with any other objects (obstacles or other modules of the network). Although the TZ structures are three-dimensional, in this paper, the problem of planar layout of the multi-branched network is considered.

At first, a simple and robust backtracking-based algorithm is demonstrated. Since it finds the first allowable solution, that is a local optimum, the configuration is generated in a short time. Such a solution, however, is most likely not the best globally. Next, an evolutionary algorithm is implemented. The encoding of a planar multi-branched network of TZ, the selection method, the cost function and the genetic operations are introduced. A number of trials have been performed, and the results are briefly discussed and interpreted.

Keywords: Truss-Z, modular ramp system, layout optimization, multi-branched network.

1. INTRODUCTION

Truss-Z (TZ) is a concept of a modular skeletal system for creating free-form transportation links and networks among any number of terminals in space [1,2]. TZ is intended for pedestrians, especially ones with strollers or carts, wheelchairs, cyclists etc. In other words, for people who have difficulties using regular stairs. The underlying idea of this system is to create structurally sound provisional or permanent structures at the minimal number of types of modular elements. The TZ structures are composed of only two units – R and L which are mirror reflection of each other. By rotation, they can be assembled in two additional ways (R₂ – rotated R and L₂ – rotated L), effectively giving effectively there are four possible types of units. Some examples are shown in figure 1.
Figure 1. Some basic examples of single-branch TZ structures. From the left: “straight and flat” with 8 units, “straight up & down” (8), a flat ring (12), and a spiral (12).

Most importantly, TZ allows automated creation of optimal structural linkages for given terminals and obstacles [3]. The optimization criteria can be the minimal number of units, in case of multiple branches – minimal network distance etc. Efficient algorithms for two-dimensional single-branch TZ linkages in constrained environment have been demonstrated [4,5]. It is also possible to create a multi-branched TZ networks as shown in figure 2.

Figure 2. An example of a six-terminal TZ network. From the left: the isometric view of a 3D TZ structure composed of four branches and the network layout.

This paper focuses on efficient methods of laying out a TZ network starting from the terminal 1 and connecting the remaining five terminals without colliding with itself and two obstacles as shown in figure 2. The domain of the problem is reduced to 2D, thus instead of four variations of a unit there are only two: $r$ (right) corresponding to $R$ and $R_2$, and $l$ (left) corresponding to $L$ and $L_2$. Since there is an additional position for a branching unit $B$, the networks are laid out with a single trapezoidal unit that can be connected to other units in three different ways, as shown in figure 3.
Figure 3. Three possible ways of attaching a new unit: depending on the type of the previous unit the path runs straight or turns. The branching unit B can be attached to the longer base of a trapezoid only.

2. BACKTRACKING

At first a backtracking-based algorithm was implemented. The branches of the network are produced consecutively. The procedure of linking any two terminals (from Start to Goal) is defined as follows:

1. Start from the given terminal (Start)

2. At each step a unit (r or l) whose centroid is closer to the Goal is chosen.

3. If any point of the unit collides with any object, the procedure steps back, switches the last unit (r→l or l→r), and continues as in 1).

4. If any point of the unit still collides with any object, the procedure steps further back, switches the second last unit and continues as in 2) until reaching the Goal.

The adaptation of this procedure for the case with six terminals is shown in table 1.
Table 1. 1) The initial branch starts from the terminal 1 and proceeds to the closest terminal (2). 2) An available unit, that is a unit from which it is possible to construct a branching B (see figure 3) towards the next two consecutive terminals, is selected so that the sum of the distances to them is minimal. 3) From that unit branches are constructed, if possible. 4) As in 2. 5) As in 3. 6) The procedure stops when the last terminal is reached.

The procedure shown above is robust and in most cases produces quite satisfactory results. However, it is almost certain that better solutions exist. Since this method relays on partial solutions that are local minima, this method can not reach the globally optimal solution. Since the system is composed of discrete units, the number of possible combinations is always finite. However, since in the general (3D) case there are four variations of a unit \((R,R_2,L,L_2)\), the number of all configurations for a single run of the truss grows exponentially as \(4^n\), where \(n\) is the number of units. For a planar case it grows as \(2^n\). The number of possible reconfigurations is additionally upsurged by the presence of multiple branches. Thus since the search space becomes so enormous, it is natural to apply heuristic method in order to investigate whether a better or alternative configurations exist.

2. EVOLUTIONARY ALGORITHM

The implementation of a classic evolutionary algorithm (EA) requires the following:

1. encoding of the solution into a genotype, that is a list of symbols,
2. selection method,
3. operation of crossover,
4. operation of mutation,
5. formulation of the fitness function, which should consistently give higher (for maximization) or lower (for minimization – as in this example) values for better candidates.

2.1. The genotype

In order to perform genetic operations the genotype should be a one-dimensional string. However, presently, the solutions are encoded as nested lists as explained in figure 4.

![Figure 4. A genotype: {r {} {r l r {l {}{l l l l l {l{r r r l r r l r r l r }{r{r r r r l {r{r r r r r r l r} {}}}}} {}} r l}}, and the corresponding complex network layout. From each branching unit two wings can be constructed: on the left and right. An empty list {} stands for the absence of a wing.

2.2. Selection

Selection is the stage when parent solutions are chosen from a population for further breeding. The most common selection methods are the Tournament (TS) and Roulette (RS), also called fitness proportionate selection. TS is based on random selection of two candidates and choosing the better one for a parent. In RS, the parent solutions are randomly selected from the population with the probability proportional to the quality of a solution. It can not be generalized whether one of the methods is always better than another. The decision should be made for an individual problem.
2.3. Crossover

The core of EA is the assumption that the desired qualities of the individuals can be carried out and augmented by selective breeding throughout a reproduction process. The most commonly used methods are one-point (OPX) and uniform (UX) crossover. With OPX a single crossover point on both parents' genotypes is selected. All data beyond that point in either one is swapped between the two parents. With UX, the genes of one parent at selected points of the genotype (called loci) are replaced with the genes at the same loci of the other parent. In this paper the number and positions of loci are random. As with selection method, the most suitable type of crossover depends on a specific problem.

2.4. Mutation

As crossover maintains the general direction of the improvement towards the global optimal solution, the operation of mutation prevents the population from degenerating, that is excessive decrease of diversity of the individuals. In other words, it prevents the process from “getting stuck” in local optima. In this case there two types of mutation were combined:

1. Unit switch mutation (USM), where randomly selected genes are assigned the opposite value ($r \rightarrow l$ or $l \rightarrow r$). USM is controlled by two parameters – $m_p$ which controls the probability of the occurrence of a mutation, and mutation intensity ($m_I$) which determines the number of genes to be mutated.

2. Branch displacement mutation (BDM), where a number of branches is displaced along the parent branch. BDM is controlled by two parameters – number of branches to be displaced ($d_B$) and the range of displacement ($d_R$).

In general, the mutation rate should be relatively low. The fine tuning is usually done by experimentation.

2.5. Fitness (cost) function

Formulating the fitness function, which in minimization problems, as in this case, is called cost function (CF) is usually the most challenging part of the EA implementation. It does not only require knowledge particular to the considered problem, but it is also necessary to give univocal, usually numerical, evaluation of each candidate solution, including the unacceptable ones. CF in the given environment $E$ for the sequence of TZ units $S$ is formulated as an aggregate objective function (AOF), that is as weighted linear combination of parameters, as follows:

$$CF_S^E = \text{Minimize} \left( \frac{\sum_{i=1}^{t} \text{Min}[d_i]}{n_{UE}} + w_3 \sum_{v=1}^{v} P_v \right)$$
where, $n_u$ is the number of units in the TZ network,

$d_i$ is the distance from an $i^{th}$ unit of the TZ network to the $i^{th}$ terminal,

$T$ is the number of terminals, since the network starts from the terminal 1 – it is omitted in the calculations.

$n_{ue}$ is the number of unique ends towards terminals of the TZ network,

$P_v$ is the penalty of the vertex $v$ violating an obstacle, $V$ is the number of vertices violating the obstacles.

$w_1, w_2, w_3$ are the parametric weights.

The penalty is applied to the configurations where vertices of some trapezoidal units violate the obstacle areas, as visualized in figure 5.

![Figure 5. The penalty is the function of the coordinates of the units' vertices. If a vertex lies inside an obstacle, the closer it is located to the obstacle's centroid - the higher is the penalty, otherwise there is no penalty. The positions of terminals are indicated by black dots.](image)

In order to calibrate the weights $w_1...w_3$, a set of representative solutions was prepared as shown in table 2.
The weights $w_1 \ldots w_3$ from the formula (1) where adjusted, so the values of CF monotonically increase with the decreasing quality of a solution. The values are: $w_1 = 0.24$, $w_2 = 0.72$, $w_3 = 10$.

2.6. The experiments

In order to set up the parameters for EA, initially a number of small experiments have been performed. The first experiment was done for two types of selection and two types of crossover (no mutation). The results are shown in table 3.

Table 3. The average and the minimal CF of the population are shown in gray and black respectively. The size of population is 100 and so is the number of generations. The overall best CF values in each setup is shown over the plot.

As table 3 indicates, in this setup the uniform crossover (UX) gives better results than the one-point crossover (OPX). Moreover, as expected, that the lack of mutation leads to degeneration of the population. After a certain, usually rather small number of generations, there are no improvements due to the homogeneity of the candidate solutions. Table 4 collects the results of the experiments with introduced unit switch mutation (USM).
Table 4. Series of experiments with USM and various combinations of EA parameters. The setup producing the best convergence throughout the generations is framed with a thick line.

Next, the branch displacement mutation (BDM) only was implemented. Table 5 collects the results of the experiments.

Table 5. Series of experiments with BDM and various combinations of EA parameters. The setups producing the best convergence throughout the generations are framed with thick lines.

Next, a series of experiments combining both types of mutation were performed, followed by the final experiment. The results are shown in table 6.
Table 6. A series of experiments with both USM and BDM at different EA parameters. The plot for the final experiment is shown in the bottom right corner.

The result of the final experiment is shown and compared with the solution created manually and generated by backtracking in figure 6.

Figure 6. From the left: The TZ network produced by EA, backtracking and manually. The CF is shown above each solution.

3. CONCLUSIONS

Presently, the results of EA to this complex optimization problem are not fully satisfactory. However, this project is not yet completed and significant improvements are expected in the near future. Besides executing more experiments for fine-tuning of the EA parameters, the CF is to be improved to reflect the quality of solutions more adequately. Moreover, as it was already implemented for a single branch in [5] the units that “go away” from the closest proximity of the end terminal to be ignored for the CF calculations. Also the encoding of the genotypes into a one dimensional list is under consideration – this would make the genetic operations more straightforward.
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4. REFERENCES


